

Solutions

MAT 0024C
Practice for the Exam
Chapter 2 (V1)
Carson

Name: _____
Date: _____
Section: _____

Solve each equation:

1. $-7y - 6 + 9y = 6$

$$\begin{array}{r} 2y - 6 = 6 \\ +6 \quad +6 \\ \hline 2y = 12 \end{array}$$

$$\boxed{y = 6}$$

2. $4x - 5 = 3x + 17$

$$\begin{array}{r} -3x \quad -3x \\ x - 5 = 17 \end{array}$$

$$\begin{array}{r} +5 \quad 5 \\ \hline x = 22 \end{array}$$

$$\boxed{x = 22}$$

3. $7(7x + 5) = 6(8x + 3)$

$$\begin{array}{r} 49x + 35 = 48x + 18 \\ -48x \quad -48x \\ \hline x + 35 = 18 \end{array}$$

$$\begin{array}{r} -35 \quad -35 \\ \hline x = -17 \end{array}$$

$$\boxed{x = -17}$$

4. $2(x - 3) + 7x = 12$

$$\begin{array}{r} 2x - 6 + 7x = 12 \\ 9x - 6 = 12 \\ +6 \quad +6 \end{array}$$

$$9x = 18$$

$$\boxed{x = 2}$$

5. $12x - 7 - 11x = 6 + (-3)$

$$\begin{array}{r} x - 7 = 3 \\ +7 \quad 7 \\ \hline x = 10 \end{array}$$

6. $3(y + 5) = 8y$

$$\begin{array}{r} 3y + 15 = 8y \\ -3y \quad -3y \\ 15 = 5y \\ \hline 3 = y \end{array}$$

7. $3(5x - 7) = 2(7x - 3)$

$$\begin{array}{r} 15x - 21 = 14x - 6 \\ -14x \quad -14x \\ x - 21 = -6 \\ +21 \quad +21 \\ \hline x = 15 \end{array}$$

8. $9 + 2(7x - 4) = -27$

$$\begin{array}{r} 9 + 14x - 8 = -27 \\ 14x + 1 = -27 \\ -1 \quad -1 \\ 14x = -28 \\ \hline x = -2 \end{array}$$

9. $\frac{2}{3}(x-4) - 3 = \frac{x}{2} - 4$

lcd
6

$$\begin{aligned} 4(x-4) - 3(6) &= 3x - 4(6) \\ 4x - 16 - 18 &= 3x - 24 \\ 4x - 34 &= 3x - 24 \\ x &= 10 \end{aligned}$$

11. $5 - 4(x+3) - 2(2x-1) = 4x + 8$

$$\begin{aligned} 5 - 4x - 12 - 4x + 2 &= 4x + 8 \\ -8x - 5 &= 4x + 8 \\ +8x &+8x \\ -13 &= 12x \\ \frac{-13}{12} &= x \end{aligned}$$

13. $4(x+6) = 4x + 24$

$4x + 24 = 4x + 24$

all real numbers
(identity)

10. $\frac{3x}{5} - 4 = \frac{x}{3} + \frac{3}{5}$

lcd
15

$$\begin{aligned} 9x - 4(15) &= 5x + 9 \\ 9x - 60 &= 5x + 9 \\ -5x &-5x \\ 4x - 60 &= 9 \\ 4x &= 69 \\ x &= \frac{69}{4} \end{aligned}$$

12. $3(x-4) = 3x - 10$

$$\begin{aligned} 3x - 12 &= 3x - 10 \\ -12 &= -10 \\ \text{no solution} & \\ \text{contradiction} & \end{aligned}$$

14. $\frac{5}{2}x - 6 = \frac{1}{7}(x+3) + 1$

lcd
14

$$\begin{aligned} \frac{5}{2}x - 6 \cdot 14 &= 14 \cdot \frac{1}{7}(x+3) + 14(1) \\ 35x - 84 &= 2(x+3) + 14 \\ 35x - 84 &= 2x + 6 + 14 \\ 35x - 84 &= 2x + 20 \\ -2x &-2x \\ 33x - 84 &= 20 \\ +84 &+84 \\ 33x &= 104 \end{aligned}$$

Write each as an equation, using "x" for a number:
(Do not solve!)

15. The sum of four times a number and twelve is thirty four.

$4x + 12 = 34$

$33x = 104$

$x = \frac{104}{33}$

16. Three times the difference between a number and eight is equal to the quotient of the number and four.

$$3(x-8) = \frac{x}{4}$$

17. The sum of three consecutive odd integers is 105. Find the integers.

| |
|----|
| 33 |
| 35 |
| 37 |

x
x+2
x+4

$$\begin{aligned} & \text{1st + 2nd + 3rd} = 105 \\ & \# \quad \# \quad \# \\ & x + (x+2) + (x+4) = 105 \\ & 3x + 6 = 105 \quad x = 33 \\ & 3x = 99 \end{aligned}$$

18. Let $V = 2\pi rh + 2\pi r^2$

a) Solve for h

$$\begin{aligned} V &= 2\pi rh + 2\pi r^2 \\ \frac{V - 2\pi r^2}{2\pi r} &= \frac{2\pi rh}{2\pi r} \end{aligned}$$

b) Find V when r = 1 and h = 3

$$\frac{V}{2\pi r} - \frac{2\pi r^2}{2\pi r} = h$$

$$\begin{aligned} V &= 2\pi rh + 2\pi r^2 \\ V &= 2\pi(1)(3) + 2\pi(1)^2 \\ V &= 6\pi + 2\pi = 8\pi \end{aligned}$$

19. Let $3x + 2y = 6$

a) Solve for y

$$\begin{aligned} 3x + 2y &= 6 \\ 2y &= 6 - 3x \\ y &= \frac{6 - 3x}{2} \end{aligned}$$

b) Find y when x = 4

$$y = \frac{3 - 3x}{2}$$

$$y = \frac{3 - 3(4)}{2} = \frac{3 - 12}{2} = \frac{-9}{2} = -4.5$$

20. Solve $P = 2L + 2W$ for L

$$P - 2W = 2L$$

$$\frac{P}{2} - W = L$$

21. Solve $C = 4xy + yd - 3k$ for d

$$C - 4xy + 3k = yd$$

$$\frac{C}{y} - \frac{4xy}{y} + \frac{3k}{y} = \frac{yd}{y}$$

$$\frac{C}{y} - 4x + \frac{3k}{y} = d$$

Solve and graph (on a number line) each of the following:

Write your answer in interval notation.

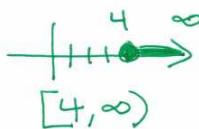
22. $4(x + 1) \leq 8x - 8 - 4$

$$4x + 4 \leq 8x - 12$$
$$-8x \quad -8x$$

$$-4x + 4 \leq -12$$
$$-4 \quad -4$$

$$-4x \leq -16$$

$$x \geq 4$$



23. $10 < 5x + 5 < 20$

$$-5 \quad -5 \quad -5$$

$$5 < 5x < 15$$

$$\frac{5}{5} < \frac{5x}{5} < \frac{15}{5}$$

$$1 < x < 3$$



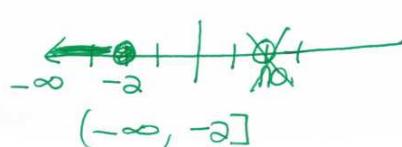
24. $(6x - 2) - 2(4x + 1) \geq 0$

$$6x - 2 - 8x - 2 \geq 0$$

$$-2x - 4 \geq 0$$

$$-2x \geq 4$$

$$x \leq -2$$



25. $6x + 5 \leq -7$

$$-5 \quad -5$$

$$6x \leq -12$$

$$x \leq -2$$

